

VIDYA BHAWAN BALIKA VIDYA PITH

शक्तिउत्थानआश्रमलखीसरायबिहार

Class-09

Sub-.Maths

Date 27.06..2021

5. In Fig. 6.43, if $PQ \perp PS$, $PQ \parallel SR$, $\angle SQR = 28^\circ$ and $\angle QRT = 65^\circ$, then find the values of x and y .

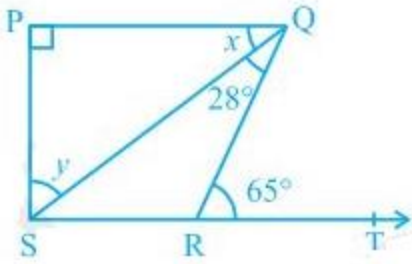


Fig. 6.43

Solution:

$x + \angle SQR = \angle QRT$ (As they are alternate angles since QR is transversal)

$$\text{So, } x + 28^\circ = 65^\circ$$

$$\therefore x = 37^\circ$$

It is also known that alternate interior angles are same and so,

$$\angle QSR = x = 37^\circ$$

Also, Now,

$$\angle QSR + \angle QRT = 180^\circ \text{ (As they are a Linear pair)}$$

$$\text{Or, } \angle QSR + 65^\circ = 180^\circ$$

$$\text{So, } \angle QSR = 115^\circ$$

Now, we know that the sum of the angles in a quadrilateral is 360° . So,

$$\angle P + \angle Q + \angle R + \angle S = 360^\circ$$

Putting their respective values, we get,

$$\angle S = 360^\circ - 90^\circ - 65^\circ - 115^\circ$$

In $\triangle SPQ$

$$\angle SPQ + x + y = 180^\circ$$

$$90^\circ + 37^\circ + y = 180^\circ$$

$$y = 180^\circ - 127^\circ = 53^\circ$$

Hence, $y = 53^\circ$

6. In Fig. 6.44, the side QR of ΔPQR is produced to a point S. If the bisectors of PQR and PRS meet at point T, then prove that $\angle QTR = \frac{1}{2} \angle QPR$.

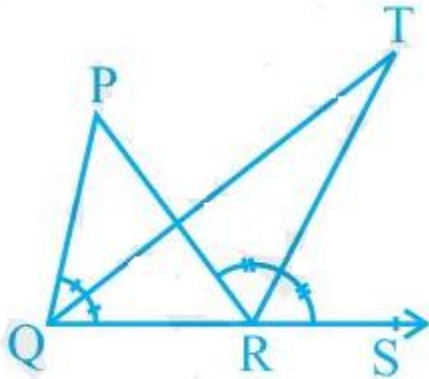


Fig. 6.44

Solution:

Consider the ΔPQR . PRS is the exterior angle and QPR and PQR are interior angles.

So, $\angle PRS = \angle QPR + \angle PQR$ (According to triangle property)

$$\text{Or, } \angle PRS - \angle PQR = \angle QPR \text{ -----(i)}$$

Now, consider the ΔQRT ,

$$\angle TRS = \angle TQR + \angle QTR$$

$$\text{Or, } \angle QTR = \angle TRS - \angle TQR$$

We know that QT and RT bisect $\angle PQR$ and $\angle PRS$ respectively.

$$\text{So, } \angle PRS = 2 \angle TRS \text{ and } \angle PQR = 2 \angle TQR$$

$$\text{Now, } \angle QTR = \frac{1}{2} \angle PRS - \frac{1}{2} \angle PQR$$

$$\text{Or, } \angle QTR = \frac{1}{2} (\angle PRS - \angle PQR)$$

From (i) we know that $\angle PRS - \angle PQR = \angle QPR$

So, $QTR = \frac{1}{2} QPR$ (hence